- De don't know if there is some w, z with >x or <x edge-disjoint paths
  - However, we do know that at most, F must be x-edge connected
  - Since vertex connectivity is bounded above by edge connectivity, Fis also at most x-connected

$$K'(G) \leq X$$

14 (G) 4 K'(G) 4 X

Cas G 13 defined to be connected.

2-	We	know	tha	+	the	number	of
	edg	e-disjo	true	Po	aths	bounds	
	edg	e-conn	ectr	V	to		

- We seck some minimum set of edge-disjoint paths for some u, v to get the edge-connectivity of G

Pseudo code:

Get Connetivity (Groph G) min Size = 00

for all u ∈ V(G) for all v ∈ V(G), v ≠ u

paths = getAllPaths (G, u, v)
if paths. size() < min Size
min Size = paths. size()

return min Size

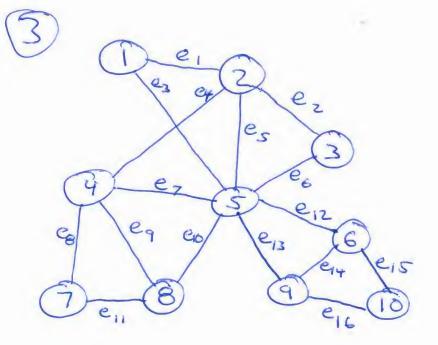
complexity = |V||V|(|V|+|E|)

nested loops assumption for

get AllPaths()

 $\approx O(n^3)$ 

polynamial time



- We observe that vertex 5 is a cut vertex, so no open-ear decomposition exists

- The graph is connected however, so we have K(G)=1

Closed-car de composition:

Po= {e, eze e3} - All ears open except

P, = { e, e, e, e, e, e, e, } for Ps

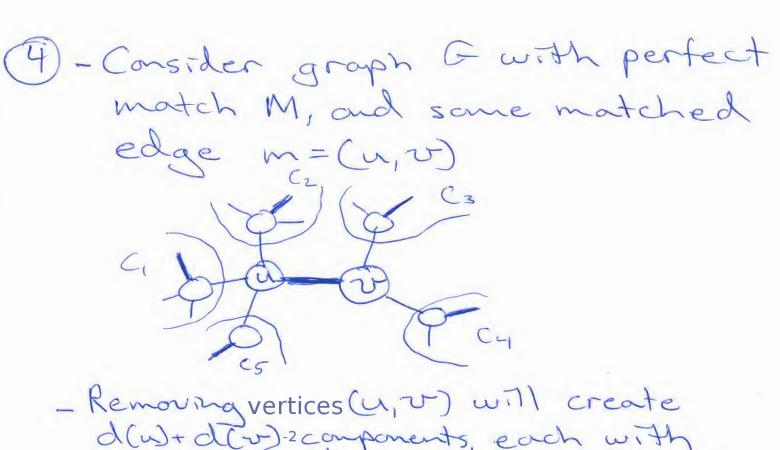
- G has a closed-ear P, = {e=} decaposition, so G

P3 = {e7} 13 2-edge-connected

P4 = 2 e 93

|K,(e)=5|P5 = {e12 e15 e16 e13}

P = { e 14}



- Removing vertices (u, v) will create d(w)+d(v)-2 components, each with a perfect match therefore even number of vertices

- If our match M is not unique, then
for some such (u,v) there exists a
match without (u,v) but with

of m, = (u,x) and m=(v,y)

- Consider C, +u, a component with a perfect match in G-(u,v) where x & V(C,)

As edge (u,x) now saturates x, we now have a subgraph of G with an odd number of vertices and can therefore not be perfectly matched

YveV(G): d(v) is even iff
for all Bz, Yuelled: dlw) is even,
where Bz are maximal biconnected
componients
HBz, HuEV(Bz): d(w) even
=7 4v + V(G): d(v) is even

- -Obviously, for a UEBz which are not orticulation points, the degrees in a BiCC and G will both be even
- For orticulation points, their degree in E is the sum of degrees in each BICC, and a sum of even numbers will necessarily also be even
- if  $\forall v \in V(G)$ : d(v) is even =>  $\forall \theta_2$ ,  $\forall u \in V(\theta_2)$ : d(u) is even
- We'll do induction on the number of Bills in G
- Pase: one BiCC -> obviously as Bi=G then Yue (B):d(u) = Yv EV(G):d(v)

From Some P(k) = H with k B-CCs and even degrees M H, all O.C.C.s taken as subgraphs have even dogras Step: We sonsider some P(n) = G with nok Biccs - We create H by removing some B; with at most one articulation point - We invoke I.H. on H - We consider adding & back into G to show our hypothesis holds Case 1: Bi was disconnected from the rest of G, its removal didn't affect ony degrees in H and its degrees in G and internal to itself or equal seven Case Z: Bi was connected to E through some articulation point as. By the degree sum formula it must have an even number of edges in Bz and also the rest of G. We mucke our I.H. on G-Bz. We then note that adding back Bi does not laffect degrees in any other vertex except az, which we already know most be